

6. $\ln y = x \ln \cos x$

$$\frac{y'}{y} = \ln \cos x + x \cdot \frac{1}{\cos x} \cdot (-\sin x)$$

$$y \cdot \frac{y'}{y} = \left(\ln \cos x - x \frac{\sin x}{\cos x} \right) y$$

$$y' = (\ln \cos x - x \tan x) (\cos x)^x$$

7a. $h' = 28 - 9.8t$

$$h'(3) = 28 - 9.8(3) = \boxed{-1.4 \text{ m/s}}$$

7b. $h = 0$

$$-4.9t^2 + 28t + 6 = 0$$

Quadratic Formula:

$$t = \frac{-28 \pm \sqrt{28^2 - 4(-4.9)(6)}}{2(-4.9)}$$

$$= \frac{-28 \pm \sqrt{901.6}}{-9.8}$$

$$t = \frac{-28 + \sqrt{901.6}}{-9.8} \text{ or } t = \frac{-28 - \sqrt{901.6}}{-9.8}$$

$$\approx -0.207$$

$$\boxed{t \approx 5.925}$$

7c. $h'(5.92) = 28 - 9.8(5.92)$

$$= \boxed{-30.016 \text{ m/s}}$$

8a. $y = Ce^{kt}$

$$580 = 200e^{k(1)}$$

$$\frac{580}{200} = \frac{200e^k}{200}$$

$$2.9 = e^k$$

$$\ln 2.9 = k \ln e$$

$$\ln 2.9 = k \text{ since } \ln e = 1$$

$$y = Ce^{\ln 2.9 t}$$

$$y = 200(e^{\ln 2.9})^t$$

$$\boxed{y = 200(2.9)^t}$$

8b. $y(5) = 200(2.9)^5$

$$\approx \boxed{41022 \text{ cells}}$$

8c. $y' = ky$

$$y' = (\ln 2.9)(200)(2.9)^t$$

$$y'(5) = (\ln 2.9)(200)(2.9)^5$$

$$\approx \boxed{43677 \text{ cells/hr}}$$

8d. $y = 80000$

$$80000 = 200(2.9)^t$$

$$\frac{80000}{200} = \frac{200(2.9)^t}{200}$$

$$400 = (2.9)^t$$

$$\frac{\ln 400}{\ln 2.9} = \frac{t \ln 2.9}{\ln 2.9}$$

$$5.63 \approx t$$

$$\boxed{\text{About } 5.63 \text{ hours}}$$